INTRODUCTION

This study examines a number of macro variables that represent domestic and foreign influences on bilateral imports to the US from Canada, Japan, and the UK. Through a vector auto regression (VAR) model with short run restrictions, the study is able to determine the importance of shocks from selected macro variables in influencing the fluctuations of bilateral imports to the US over different time horizons.

The study is based off Koray & Lastrapes’ paper Real Exchange Rate Volatility on U.S. Bilateral Trade: A VAR Approach (1989), which uses the same VAR model to investigate the impact of real exchange rate volatility on U.S. bilateral imports before and after the Bretton Woods system, up until 1985. Due to the availability of bilateral data, I will be extending their study and only examine data from 1985 to the present day. Furthermore, instead of just focusing on the relationship between exchange rate volatility and bilateral imports, I will be considering shocks from the entire system.

VAR THEORY

Vector Autoregression (VAR) is a procedure for examining how shocks to the variables in a system affect the system over time. The key attribute of the multi-equation approach through VAR is that the variables in the system are completely endogenous. The improvements VAR makes on single equation time-series methods has placed VAR in the limelight of contemporary time-series research.

The VAR model can be easily understood by examining a simple bivariate system with one lag:

1.) Consider 2 equations that explain the system of two variables $y_1$ and $y_2$.

$$y_{1t} = \phi_{11} y_{1t-1} + \phi_{12} y_{2t-1} + \epsilon_{1t}$$

$$y_{2t} = \phi_{21} y_{1t-1} + \phi_{22} y_{2t-1} + \epsilon_{2t}$$

Where $\epsilon_{1t} \sim N(0, \sigma_1^2)$

$$\epsilon_{2t} \sim N(0, \sigma_2^2)$$

2.) Taking the left product of the inverse matrix of $B$ and then by letting $C = B^{-1} \Gamma_1$ and $\phi = B^{-1} \Gamma_2$, the equation is now in a form that an OLS regression can produce parameter estimates.

$$Y_t = C + \Phi \epsilon_{t-1} + \eta_t$$

3.) The estimation of the reduced form model yields a total of nine parameters estimates:

$$\hat{C} \text{, } \hat{\Phi} \text{, } \hat{\phi} \text{, } \hat{\sigma}_1^2 \text{, } \hat{\sigma}_2^2$$

However, the original system of equations contains ten parameters.

$\gamma_{1t} = \phi_{11} \gamma_{1t-1} + \phi_{12} \gamma_{2t-1}$

In order to exactly identify the system, econometricians use either Short-Run, Long-Run, or Sign Restrictions.

4.) The VAR reduced form model in (2) can be transformed into a moving average (MA) model where each variable in the system is a function of contemporaneous and lagged orthogonal shocks.

$$Y_t = H + (L + \phi_1 L^2 + \ldots + \phi_{L} L^L) \epsilon_t + \epsilon_t$$

(Wold MA form)

In the Wold MA Form, the VAR results can be analyzed in two ways:

1. Variance Decomposition shows the proportion of variability of a variable that is attributed to different shocks (c) in the system over different time horizons.

2. Impulse Response Functions depict the response of variables to a one standard deviation shock in a specific variable.

RESUL TS

In the VAR approach through VAR is that the variables in the system are completely endogenous. Therefore, the study is based off Koray & Lastrapes’ paper Real Exchange Rate Volatility on U.S. Bilateral Trade: A VAR Approach (1989), which uses the same VAR model to investigate the impact of real exchange rate volatility on U.S. bilateral imports before and after the Bretton Woods system, up until 1985. Due to the availability of bilateral data, I will be extending their study and only examine data from 1985 to the present day. Furthermore, instead of just focusing on the relationship between exchange rate volatility and bilateral imports, I will be considering shocks from the entire system.

Variables without an * represent U.S. variables while variables with an * represents foreign variables:

• M, M*: M1 money supply
• R, R*: Long Term Government Bond Yield
• P, P*: Consumer Price Index
• Y, Y*: Industrial Production Index
• S: Nominal Exchange Rate
• IMP: Bilateral Imports to the US
• V: Real Exchange Rate Volatility

The VAR identifies orthogonal shocks through the use of short run restrictions, with the ordering:


The ordering is determined by the intuition that US, being a large economy, responds more sluggishly to shocks emanating from a smaller country.

REFERENCES


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